# Package ‘debCAM' 

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Description An R package for fully unsupervised deconvolution of complex tissues. It provides basic functions to perform unsupervised deconvolution on mixture expression profiles by Convex Analysis of Mixtures (CAM) and some
auxiliary functions to help understand the subpopulation-specific results. It also implements functions to perform supervised deconvolution based on prior knowledge of molecular markers, S matrix or A matrix. Combining molecular markers from CAM and from prior knowledge can achieve semi-supervised deconvolution of mixtures.
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## R topics documented:

debCAM-package ..... 2
AfromMarkers ..... 3
AS-accessor ..... 4
CAM ..... 5
CAMASest ..... 7
CAMASObj-class ..... 9
CAMMGCluster ..... 10
CAMMGObj-class ..... 11
CAMObj-class ..... 11
CAMPrep ..... 12
CAMPrepObj-class ..... 14
cornerSort ..... 14
MDL ..... 15
MDLObj-class ..... 16
MGsforA ..... 17
MGstatistic ..... 18
PCAmat ..... 19
ratMix3 ..... 20
redoASest ..... 20
reselectMG ..... 22
sffsHull ..... 23
simplexplot ..... 24
XWProj ..... 26
Index ..... 27
debCAM-package debCAM: A package for fully unsupervised deconvolution of complex
tissues.

## Description

The core function in this package is CAM which achieves fully unsupervised deconvolution on mixture expression profiles. Each step in CAM can also be performed separately by CAMPrep, CAMMGCluster and CAMASest in a more flexible workflow. MGstatistic can help extract a complete marker list from CAM results. MDL can help decide the underlying subpopulation number. With other functions, e.g. AfromMarkers and MGstatistic, this package can also perform supervised deconvolution based on prior knowledge of molecular markers, subpopulation-specific expression matrix (S) or proportion matrix (A). Semi-supervised deconvolution can be achieved by combining molecular markers from CAM and from prior knowledge to analyze mixture expressions.

## References

Wang, N., Hoffman, E. P., Chen, L., Chen, L., Zhang, Z., Liu, C., ... Wang, Y. (2016). Mathematical modelling of transcriptional heterogeneity identifies novel markers and subpopulations in complex tissues. Scientific Reports, 6, 18909. http://doi.org/10.1038/srep18909

## AfromMarkers Proportion matrix estimation from marker genes

## Description

This function estimates proportion matrix (A matrix) from observed mixture expression data based on marker genes.

## Usage

AfromMarkers(data, MGlist, scaleRecover = TRUE)

## Arguments

data A data set that will be internally coerced into a matrix. Each row is a gene and each column is a sample. data should be in non-log linear space with nonnegative numerical values (i.e. $>=0$ ). Missing values are not supported. All-zero rows will be removed internally.
MGlist A list of vectors, each of which contains known markers and/or CAM-detected markers for one subpopulation.
scaleRecover If TRUE, scale ambiguity of each column vector in A matrix is removed based on sum-to-one constraint on each row.

## Details

With the expression levels of subpopulation-specific marker genes, the relative proportions of constituent subpopulations are estimated by spatial median using 11 median. Marker genes could be from unsupervised/supervised detection or from literatures. Scale ambiguity is optionally removed based on sum-to-one constraint of rows.

## Value

Return the estimated proportion matrix (A matrix).

## Examples

```
#obtain data and marker genes
data(ratMix3)
S <- ratMix3$S
pMGstat <- MGstatistic(S, c("Liver","Brain","Lung"))
pMGlist.FC <- lapply(c("Liver","Brain","Lung"), function(x)
    rownames(pMGstat)[pMGstat$idx == x & pMGstat$OVE.FC > 10])
```

\#estimate A matrix from markers
Aest <- AfromMarkers(ratMix3\$X, pMGlist.FC)

AS-accessor Deconvoluted matrix accessors

## Description

Accessors to proportion matrix and subpopulation-specific expression matrix estimated by CAM.

## Usage

> Amat (x, ...)

Smat (x, ...)
\#\# S4 method for signature 'CAMObj'
Amat (x, k, usingPCA = TRUE)
\#\# S4 method for signature 'CAMASObj'
Amat (x, usingPCA = TRUE)
\#\# S4 method for signature 'CAMObj'
Smat ( $\mathrm{x}, \mathrm{k}$, usingPCA = TRUE)
\#\# S4 method for signature 'CAMASObj'
Smat ( $x$, usingPCA $=$ TRUE )

## Arguments

x
... additional argument list.
$k \quad$ subpopulation number
usingPCA If TRUE, A matrix is estimated by transforming dimension-reduced A matrix back to original space. Otherwise, A matrix is directly estimated in original data space. The default is TRUE.

## Value

Estimated A matrix or S matrix.

## Examples

```
#obtain data
data(ratMix3)
data <- ratMix3$X
rCAM <- CAM(data, K = 3, dim.rdc = 3, thres.low = 0.30, thres.high = 0.95)
Aest <- Amat(rCAM, 3)
Sest <- Smat(rCAM, 3)
Aest <- Amat(slot(rCAM, "ASestResult")[[1]])
Sest <- Smat(slot(rCAM, "ASestResult")[[1]])
```

CAM Convex Analysis of Mixtures

## Description

This function performs a fully unsupervised computational deconvolution to identify marker genes that define each of the multiple subpopulations, and estimate the proportions of these subpopulations in the mixture tissues as well as their respective expression profiles.

## Usage

CAM(data, K = NULL, corner.strategy = 2, dim.rdc = 10,
thres.low $=0.05$, thres.high $=0.95$, cluster.method $=c(" K-M e a n s "$,
"apcluster"), cluster.num = 50, MG.num.thres $=20$,
lof.thres $=0.02$, quickhull $=$ TRUE, quick.select $=$ NULL,
sample.weight $=$ NULL, appro3 $=$ TRUE, generalNMF = FALSE,
cores = NULL)

## Arguments

$$
\begin{array}{ll}
\text { data } & \begin{array}{l}
\text { Matrix of mixture expression profiles. Data frame, SummarizedExperiment or } \\
\text { ExpressionSet object will be internally coerced into a matrix. Each row is a } \\
\text { gene and each column is a sample. Data should be in non-log linear space with } \\
\text { non-negative numerical values (i.e. }>=0 \text { ). Missing values are not supported. } \\
\text { All-zero rows will be removed internally. }
\end{array} \\
\text { K } & \begin{array}{l}
\text { The candidate subpopulation number(s), e.g. } \mathrm{K}=2: 8 .
\end{array} \\
\text { corner.strategy }
\end{array} \quad \begin{aligned}
& \text { The method to find corners of convex hull. } 1: \text { minimum sum of margin-of- } \\
& \text { errors; 2: minimum sum of reconstruction errors. The default is } 2 .
\end{aligned}
$$

$$
\begin{array}{ll}
\text { cluster.method } & \begin{array}{l}
\text { The method to do clustering. The default "K-Means" will use kmeans. The } \\
\text { alternative "apcluster" will use apclusterK-methods. }
\end{array} \\
\text { cluster.num } & \begin{array}{l}
\text { The number of clusters; should be much larger than K. The default is 50. } \\
\text { MG. num. thres } \\
\text { The clusters with the gene number smaller than MG.num.thres will be treated as } \\
\text { outliers. The default is 20. }
\end{array} \\
\text { lof.thres } & \begin{array}{l}
\text { Remove local outlier using lofactor. MG.num.thres is used as the number of } \\
\text { neighbors in the calculation of the local outlier factors. The default value } 0.02 \\
\text { will remove top 2\% local outliers. Zero value will disable lof. }
\end{array} \\
\text { quickhull } & \begin{array}{l}
\text { Perform quickhull to select clusters or not. The default is True. }
\end{array} \\
\text { quick. select } & \begin{array}{l}
\text { The number of candidate corners kept after quickhull and SFFS greedy search. } \\
\text { If Null, only quickhull is applied. The default is 20. If this value is larger than } \\
\text { the number of candidate corners after quickhull, greedy search will also not be } \\
\text { applied. }
\end{array} \\
\text { sample.weight } & \begin{array}{l}
\text { Vector of sample weights. If NULL, all samples have the same weights. The } \\
\text { length should be the same as sample numbers. All values should be positive. }
\end{array} \\
\text { appro3 } & \begin{array}{l}
\text { Estimate A and S matrix by approach } 3 \text { or not. Please see CAMASest for further } \\
\text { information. The default is TRUE. }
\end{array} \\
\text { generalNMF } & \begin{array}{l}
\text { If TRUE, the decomposed proportion matrix has no sum-to-one constraint for } \\
\text { each row. The default is FALSE. TRUE value brings two changes: (1) Without } \\
\text { assuming samples are normalized, the first principal component will not forced } \\
\text { to be along c(1,1,.., but a standard PCA will be applied during preprocessing. } \\
\text { (2) Without sum-to-one constraint for each row, the scale ambiguity of each } \\
\text { column vector in proportion matrix will not be removed. }
\end{array} \\
\text { The number of system cores for parallel computing. If not provided, one core for } \\
\text { each element in K will be invoked. Zero value will disable parallel computing. }
\end{array}
$$

## Details

This function includes three necessary steps to decompose a matrix of mixture expression profiles: data preprocessing, marker gene cluster search, and matrix decomposition. They are implemented in CAMPrep, CAMMGCluster and CAMASest, separately. More details can be found in the help document of each function.
For this function, you needs to specify the range of possible subpopulation numbers and the percentage of low/high-expressed genes to be removed. Typically, $30 \% \sim 50 \%$ low-expressed genes can be removed from gene expression data. The removal of high-expressed genes has much less impact on results, and usually set to be $0 \% \sim 10 \%$.
This function can also analyze other molecular expression data, such as proteomics data. Much less low-expressed proteins need to be removed, e.g. $0 \% \sim 10 \%$, due to a limited number of proteins without missing values.

## Value

An object of class "CAMObj" containing the following components:
PrepResult An object of class "CAMPrepObj" containing data preprocessing results from CAMPrep function.

| MGResult | A list of "CAMMGObj" objects containing marker gene detection results from <br> CAMMGCluster function for each K value. |
| :--- | :--- |
| ASestResult | A list of "CAMASObj" objects containing estimated proportions, subpopulation- <br> specific expressions and mdl values from CAMASest function for each K value. |

## Examples

```
    #obtain data
    data(ratMix3)
    data <- ratMix3$X
    #set seed to generate reproducible results
    set.seed(111)
    #CAM with known subpopulation number
    rCAM <- CAM(data, K = 3, dim.rdc = 3, thres.low = 0.30, thres.high = 0.95)
    #Larger dim.rdc can improve performance but increase time complexity
    ## Not run:
    #CAM with a range of subpopulation number
    rCAM <- CAM(data, K = 2:5, dim.rdc = 10, thres.low = 0.30, thres.high = 0.95)
    #Use "apcluster" to aggregate gene vectors in CAM
    rCAM <- CAM(data, K = 2:5, dim.rdc = 10, thres.low = 0.30, thres.high = 0.95,
    cluster.method = 'apcluster')
    #CAM with quick selection to reduce time complexity
    rCAM <- CAM(data, K = 3, dim.rdc = 10, thres.low = 0.30, thres.high = 0.95,
        quick.select = 20)
    #CAM with different sample weights (e.g. adjusted based on sample quality)
    rCAM <- CAM(data, K = 3, dim.rdc = 5, thres.low = 0.30, thres.high = 0.95,
        sample.weight = c(rep(10,11),rep(1,10)))
#CAM for general NMF (no sum-to-one contraint for proportion matrix)
rCAM <- CAM(data, K = 3, dim.rdc = 5, thres.low = 0.30, thres.high = 0.95,
        generalNMF = TRUE)
## End(Not run)
```

CAMASest $\quad A$ and $S$ matrix estimation by CAM

## Description

This function estimates A and S matrix based on marker gene clusters detected by CAM.

## Usage

CAMASest(MGResult, PrepResult, data, corner.strategy $=2$, appro3 $=$ TRUE, generalNMF $=$ FALSE)

## Arguments

$$
\begin{array}{ll}
\text { MGResult } & \text { An object of class "CAMMGObj" obtained from CAMMGCluster function. } \\
\text { PrepResult } & \text { An object of class "CAMPrepObj" obtained from CAMPrep function. } \\
\text { data } & \begin{array}{l}
\text { Matrix of mixture expression profiles which need to be the same as the input } \\
\text { of CAMPrep. Data frame, SummarizedExperiment or ExpressionSet object will } \\
\text { be internally coerced into a matrix. Each row is a gene and each column is a } \\
\\
\\
\\
\\
\\
\\
\text { sample. Data should be in non-log linear space with non-negative numerical } \\
\text { values (i.e. >=0). Missing values are not supported. All-zero rows will be } \\
\\
\text { removed internally. }
\end{array}
\end{array}
$$

corner.strategy
The method to detect corner clusters. 1: minimum sum of margin-of-errors; 2: minimum sum of reconstruction errors. The default is 2 .
appro3 Estimate A and S matrix by approach 3 or not. Please see details for further information. The default is TRUE.
generalNMF If TRUE, the decomposed proportion matrix has no sum-to-one constraint for each row. Without this constraint, the scale ambiguity of each column vector in proportion matrix will not be removed. The default is FALSE.

## Details

This function is used internally by CAM function to estimate proportion matrix (A), subpopulationspecific expression matrix ( S ) and mdl values. It can also be used when you want to perform CAM step by step.
The mdl values are calculated in three approaches: (1) based on data and A matrix in dimensionreduced space; (2) based on original data with A matrix estimated by transforming dimensionreduced A matrix back to original space; (3) based on original data with A directly estimated in original space. A and $S$ matrix in original space estimated from the latter two approaches are returned. mdl is the sum of two terms: code length of data under the model and code length of model. Both mdl value and the first term (code length of data) will be returned.

## Value

An object of class "CAMASObj" containing the following components:

| Aest | Estimated proportion matrix from Approach 2. |
| :--- | :--- |
| Sest | Estimated subpopulation-specific expression matrix from Approach 2. |
| Aest.proj | Estimated proportion matrix from Approach 2, before removing scale ambigu- <br> ity. |
| Ascale | The estimated scales to remove scale ambiguity of each column vector in Aest. <br> Sum-to-one constraint on each row of Aest is used for scale estimation. |
| Aest0 | Estimated proportion matrix from Approach 3. |
| Sest0 | Estimated subpopulation-specific expression matrix from Approach 3. |
| Aest0.proj | Estimated proportion matrix from Approach 3, before removing scale ambigu- <br> ity. |

$$
\begin{array}{ll}
\text { Ascale0 } & \begin{array}{l}
\text { The estimated scales to remove scale ambiguity of each column vector in AestO. } \\
\text { Sum-to-one constraint on each row of AestO is used for scale estimation. }
\end{array} \\
\text { datalength } & \begin{array}{l}
\text { Three values for code length of data. The first is calculated based on dimension- } \\
\text { reduced data. The second and third are based on the original data. }
\end{array} \\
\text { mdl } & \begin{array}{l}
\text { Three mdl values. The first is calculated based on dimension-reduced data. The } \\
\text { second and third are based on the original data. }
\end{array}
\end{array}
$$

## Examples

```
#obtain data
data(ratMix3)
data <- ratMix3$X
#preprocess data
rPrep <- CAMPrep(data, dim.rdc = 3, thres.low = 0.30, thres.high = 0.95)
#Marker gene cluster detection with a fixed K
rMGC <- CAMMGCluster(3, rPrep)
#A and S matrix estimation
rASest <- CAMASest(rMGC, rPrep, data)
```

CAMASObj-class Class "CAMASObj"

## Description

An S4 class for storing estimated proportions, subpopulation-specific expressions and mdl values. The mdl values are calculated in three approaches: (1) based on data and A matrix in dimensionreduced space; (2) based on original data with A matrix estimated by transforming dimensionreduced A matrix back to original space; (3) based on original data with A directly estimated in original space. A and $S$ matrix in original space estimated from the latter two approaches are returned. mdl is the sum of two terms: code length of data under the model and code length of model. Both mdl value and the first term (code length of data) will be returned.

## Slots

Aest Estimated proportion matrix from Approach 2.
Sest Estimated subpopulation-specific expression matrix from Approach 2.
Aest.proj Estimated proportion matrix from Approach 2, before removing scale ambiguity.
Ascale The estimated scales to remove scale ambiguity of each column vector in Aest. Sum-to-one constraint on each row of Aest is used for scale estimation.
Aest0 Estimated proportion matrix from Approach 3.
Sest0 Estimated subpopulation-specific expression matrix from Approach 3.
Aest0.proj Estimated proportion matrix from Approach 3, before removing scale ambiguity.

Ascale0 The estimated scales to remove scale ambiguity of each column vector in AestO. Sum-toone constraint on each row of AestO is used for scale estimation.
datalength Three values for code length of data. The first is calculated based on dimensionreduced data. The second and third are based on the original data.
mdl Three mdl values. The first is calculated based on dimension-reduced data. The second and third are based on the original data.

## CAMMGCluster MG cluster detection for CAM

## Description

This function finds corner clusters as MG clusters (clusters containing marker genes).

## Usage

CAMMGCluster (K, PrepResult, generalNMF = FALSE, nComb $=200$ )

## Arguments

K
PrepResult
generalNMF
The candidate subpopulation number.
An object of class "CAMPrepObj" obtained from CAMPrep function.
If TRUE, the decomposed proportion matrix has no sum-to-one constraint for each row. Without this constraint, the scale ambiguity of corner cluster centers will not be removed when computing reconstruction errors. The default is FALSE.
nComb The number of possible combinations of clusters as corner clusters. Within these possible combinations ranked by margin errors, we can further select the best one based on reconstruction errors. The default is 200.

## Details

This function is used internally by CAM function to detect clusters containing marker genes, or used when you want to perform CAM step by step.
This function provides two solutions. The first is the combination of clusters yielding the minimum sum of margin-of-errors for cluster centers. In the second, nComb possible combinations are selected by ranking sum of margin-of-errors for cluster centers. Then the best one is selected based on reconstruction errors of all data points in original space.

## Value

An object of class "CAMMGObj" containing the following components:

| idx | Two numbers which are two solutions' ranks by sum of margin-of-error. |
| :--- | :--- |
| corner | The indexes of clusters as detected corners. Each row is a solution. |
| error | Two rows. The first row is sum of margin-of-errors for nComb possible combi- <br> nations. The second row is reconstruction errors for nComb possible combina- <br> tions. |

## Examples

```
#obtain data
data(ratMix3)
data <- ratMix3$X
#preprocess data
rPrep <- CAMPrep(data, dim.rdc = 3, thres.low = 0.30, thres.high = 0.95)
    #Marker gene cluster detection with a fixed K = 3
    rMGC <- CAMMGCluster(3, rPrep)
```

CAMMGObj-class Class "CAMMGObj"

## Description

An S4 class for storing marker gene detection results.

## Slots

idx Two numbers which are two solutions' ranks by sum of margin-of-error.
corner The indexes of clusters as detected corners. Each row is a solution.
error Two rows. The first row is sum of margin-of-errors for nComb possible combinations. The second row is reconstruction errors for nComb possible combinations.
CAMObj-class Class "CAMObj"

## Description

An S4 class for storing results of CAM.

## Slots

PrepResult An object of class "CAMPrepObj" storing data preprocessing results from CAMPrep function.

MGResult A list of "CAMMGObj" objects storing marker gene detection results from CAMMGCluster function for each candidate subpopulation number.
ASestResult A list of "CAMASObj" objects storing estimated proportions, subpopulation-specific expressions and mdl values from CAMASest function for each candidate subpopulation number.

## Description

This function perform preprocessing for CAM, including norm-based filtering, dimension deduction, perspective projection, local outlier removal and aggregation of gene expression vectors by clustering.

## Usage

CAMPrep(data, dim.rdc $=10$, thres.low $=0.05$, thres.high $=0.95$, cluster.method = c("K-Means", "apcluster"), cluster.num = 50, MG.num.thres $=20$, lof.thres $=0.02$, quickhull $=$ TRUE, quick.select $=$ NULL, sample.weight $=$ NULL, generalNMF $=$ FALSE)

## Arguments

| data | Matrix of mixture expression profiles. Data frame, SummarizedExperiment or ExpressionSet object will be internally coerced into a matrix. Each row is a gene and each column is a sample. Data should be in non-log linear space with non-negative numerical values (i.e. $>=0$ ). Missing values are not supported. All-zero rows will be removed internally. |
| :---: | :---: |
| dim.rdc | Reduced data dimension; should be |
| thres.low | The lower bound of percentage of genes to keep for CAM with ranked norm. The value should be between 0 and 1 . The default is 0.05 . |
| thres.high | The higher bound of percentage of genes to keep for CAM with ranked norm. The value should be between 0 and 1 . The default is 0.95 . |
| cluster.method | The method to do clustering. The default "K-Means" will use kmeans function. The alternative "apcluster" will use apclusterK-methods. |
| cluster.num | The number of clusters; should be much larger than K. The default is 50. |
| MG.num.thres | The clusters with the gene number smaller than MG.num.thres will be treated as outliers. The default is 20 . |
| lof.thres | Remove local outlier using lofactor function. MG.num.thres is used as the number of neighbors in the calculation of the local outlier factors. The default value 0.02 will remove top $2 \%$ local outliers. Zero value will disable lof. |
| quickhull | Perform quickhull to select clusters or not. The default is True. |
| quick.select | The number of candidate corners kept after quickhull and SFFS greedy search. If Null, only quickhull is applied. The default is 20 . If this value is larger than the number of candidate corners after quickhull, greedy search will also not be applied. |
| sample.weight | Vector of sample weights. If NULL, all samples have the same weights. The length should be the same as sample numbers. All values should be positive. |

generalNMF If TRUE, the decomposed proportion matrix has no sum-to-one constraint for each row. Without assuming samples are normalized, the first principal component will not forced to be along $c(1,1, . ., 1)$ but a standard PCA will be applied during preprocessing.

## Details

This function is used internally by CAM function to preprocess data, or used when you want to perform CAM step by step.
Low/high-expressed genes are filtered by their L2-norm ranks. Dimension reduction is slightly different from PCA. The first loading vector is forced to be $c(1,1, \ldots, 1)$ with unit norm normalization. The remaining are eigenvectors from PCA in the space orthogonal to the first vector. Perspective projection is to project dimension-reduced gene expression vectors to the hyperplane orthogonal to $c(1,0, \ldots, 0)$, i.e., the first axis in the new coordinate system. local outlier removal is optional to exclude outliers in simplex formed after perspective projection. Finally, gene expression vectors are aggregated by clustering to further reduce the impact of noise/outlier and help improve the efficiency of simplex corner detection.

## Value

An object of class "CAMPrepObj" containing the following components:

| Valid | logical vector to indicate the genes left after filtering. |
| :--- | :--- |
| Xprep | Preprocessed data matrix. |
| Xproj | Preprocessed data matrix after perspective projection. |
| W | The matrix whose rows are loading vectors. |
| SW | Sample weights. <br> cluster |
| cluster results including two vectors. The first indicates the cluster to which <br> each gene is allocated. The second is the number of genes in each cluster. |  |
| centers | The clusters with the gene number smaller than MG.num.thres. <br> The centers of candidate corner clusters (candidate clusters containing marker <br> genes). |

## Examples

```
#obtain data
data(ratMix3)
data <- ratMix3$X
#set seed to generate reproducible results
set.seed(111)
#preprocess data
rPrep <- CAMPrep(data, dim.rdc = 3, thres.low = 0.30, thres.high = 0.95)
```

CAMPrepObj-class Class "CAMPrepObj"

## Description

An S4 class for storing data preprocessing results.

## Slots

Valid logical vector to indicate the genes left after filtering.
Xprep Preprocessed data matrix.
Xproj Preprocessed data matrix after perspective projection.
W The matrix whose rows are loading vectors.
cluster cluster results including two vectors. The first indicates the cluster to which each gene is allocated. The second is the number of genes in each cluster.
c. outlier The clusters with the gene number smaller than MG.num.thres.
centers The centers of candidate corner clusters (candidate clusters containing marker genes).
cornerSort Candidate combinations as corners

## Description

Given a set of data points, return possible combinations of data points as corners. These combinations are selected by ranking the sum of margin-of-errors.

## Usage

cornerSort(X, K, nComb)

## Arguments

$X \quad$ Data in a matrix. Each column is a data point.
K The number of corner points.
nComb The number of returned combinations of data points as corners. All combinations will be returned if the number of all combinations is less than nComb.

## Details

This function is to detect $K$ corner points from $M$ data points by conducting an exhaustive combinatorial search (with total $C_{M}^{K}$ combinations), based on a convex-hull-to-data fitting criterion: sum of margin-of-errors. nComb combinations are returned for further selection based on reconstruction errors of all data points in original space.
The function is implemented in Java with R-to-Java interface provided by rJava package. It relies on NonNegativeLeastSquares class in Parallel Java Library (https://www.cs.rit.edu/~ark/pj.shtml).

## Value

A list containing the following components:
idx A matrix to show the indexes of data points in combinations to construct a convex hull. Each column is one combination.
error A vector of margin-of-error sums for each combination.

## Examples

```
data <- matrix(c(0.1,0.2,1.0,0.0,0.0,0.5,0.3,
    0.1,0.7,0.0,1.0,0.0,0.5,0.3,
    0.8,0.1,0.0,0.0,1.0,0.0,0.4), nrow =3, byrow = TRUE)
topconv <- cornerSort(data, 3, 10)
```

MDL

Minimum Description Length

## Description

This function obtains minimum description length (mdl) values for each candidate subpopulation number.

## Usage

MDL(CAMResult, mdl.method = 3)
\#\# S4 method for signature 'MDLObj,missing'
plot ( $x$, data.term $=$ FALSE,.. )

## Arguments

CAMResult Result from CAM function.
mdl.method Approach to calculate mdl values; should be 1, 2, or 3. The default is 3 .
x
An object of class "MDLObj" from MDL.
data.term If true, plot data term (code length of data under model).
... All other arguments are passed to the plotting command.

## Details

This function extracts minimum description length (mdl) values from the result of CAM function, which contains mdl values form three approaches for each candidate subpopulation number. For more details about three approaches, refer to CAMASest.
mdl is code length of data under the model plus code length of model. Both mdl value and the first term about data are returned.

## Value

An object of class "MDLObj" containing the following components:

| K | The candidate subpopulation numbers. |
| :--- | :--- |
| datalengths | For each model with a certain subpopulation number, code length of data under <br> the model. |
| mdls | mdl value for each model with a certain subpopulation number. |

## Examples

```
## Not run:
#obtain data
data(ratMix3)
data <- ratMix3$X
#Analysis by CAM
rCAM <- CAM(data, K = 2:5, thres.low = 0.30, thres.high = 0.95)
#extract mdl values
MDL(rCAM)
MDL(rCAM, 1)
MDL(rCAM, 2)
#plot MDL curves
plot(MDL(rCAM))
plot(MDL(rCAM), data.term = TRUE) #with data length curve
## End(Not run)
```

```
MDLObj-class Class "MDLObj"
```


## Description

An S4 class for storing mdl values.

## Slots

K The candidate subpopulation numbers.
datalengths For each model with a certain subpopulation number, code length of data under the model.
mdls mdl value for each model with a certain subpopulation number.

## Description

This function returns marker genes detected by CAM for estimating A.

## Usage

MGsforA(CAMResult = NULL, K = NULL, PrepResult = NULL, MGResult $=$ NULL, corner.strategy $=2$ )

## Arguments

CAMResult Result from CAM.
K The candidate subpopulation number.
PrepResult An object of class "CAMPrepObj" from CAMPrep.
MGResult An object of class "CAMMGObj" from CAMMGCluster.
corner.strategy
The method to detect corner clusters. 1: minimum sum of margin-of-errors; 2: minimum sum of reconstruction errors. The default is 2 .

## Details

This function needs to specify CAMResult and K, or PrepResult and MGResult. The returned marker genes are those used by CAM for estimating A. To obtain a more complete marker gene list, please refer to MGstatistic.

## Value

A list of vectors, each of which contains marker genes for one subpopulation.

## Examples

```
#obtain data and run CAM
data(ratMix3)
data <- ratMix3$X
rCAM <- CAM(data, K = 3, dim.rdc= 3, thres.low = 0.30, thres.high = 0.95)
#obtain marker genes detected by CAM for estimating A
MGlist <- MGsforA(rCAM, K = 3)
#obtain data and run CAM step by step
rPrep <- CAMPrep(data, dim.rdc= 3, thres.low = 0.30, thres.high = 0.95)
rMGC <- CAMMGCluster(3, rPrep)
#obtain marker genes detected by CAM for estimating A
MGlist <- MGsforA(PrepResult = rPrep, MGResult = rMGC)
```


## Description

This function computes One-Versus-Everyone Fold Change (OVE-FC) from subpopulation-specific expression profiles. Bootstrapping is optional.

## Usage

MGstatistic(data, $A=$ NULL, boot.alpha $=$ NULL, nboot $=1000$, cores $=$ NULL)

## Arguments

data A data set that will be internally coerced into a matrix. Each row is a gene and each column is a sample. Data should be in non-log linear space with nonnegative numerical values (i.e. $>=0$ ). Missing values are not supported. All-zero rows will be removed internally.

A
When data are mixture expression profiles, A is estimated proportion matrix or prior proportion matrix. When data are pure expression profiles, A is a phenotype vector to indicate which subpopulation each sample belongs to.
boot.alpha Alpha for bootstrapped OVE-FC confidence interval. The default is 0.05.
nboot The number of boots.
cores The number of system cores for parallel computing. If not provided, the default back-end is used.

## Details

This function calculates OVE-FC and bootstrapped OVE-FC which can be used to identify markers from all genes.

## Value

A data frame containing the following components:
idx Numbers or phenotypes indicating which subpopulation each gene could be a marker for. If A is a proportion matrix without column name, numbers are returned. Otherwise, phenotypes.

OVE.FC One-versus-Everyone fold change (OVE-FC)
OVE.FC.alpha lower confidence bound of bootstrapped OVE-FC at alpha level.

## Examples

```
#data are mixture expression profiles, A is proportion matrix
data(ratMix3)
MGstat <- MGstatistic(ratMix3$X, ratMix3$A)
## Not run:
MGstat <- MGstatistic(ratMix3$X, ratMix3$A, boot.alpha = 0.05) #enable boot
## End(Not run)
#data are pure expression profiles without replicates
MGstat <- MGstatistic(ratMix3$S) #boot is not applicable
## Not run:
#data are pure expression profiles with phenotypes
S <- matrix(rgamma(3000,0.1,0.1), 1000, 3)
S <- S[, c(1,1,1,2,2,2,3,3,3,3)] + rnorm(1000*10, 0, 0.5)
MGstat <- MGstatistic(S, c(1,1,1,2,2,2,3,3,3,3), boot.alpha = 0.05)
## End(Not run)
```


## PCAmat Dimension-reduction loading matrix accessor

## Description

Accessor to Dimension-reduction loading matrix.

## Usage

```
PCAmat(x, ...)
## S4 method for signature 'CAMObj'
PCAmat(x)
## S4 method for signature 'CAMPrepObj'
PCAmat(x)
```


## Arguments

x
a CAMObj object or a CAMPrepObj object
... additional argument list.

## Value

The matrix whose rows are loading vectors for dimension reduction.

## Examples

```
    #obtain data
    data(ratMix3)
    data <- ratMix3$X
    rCAM <- CAM(data, K = 3, dim.rdc = 3, thres.low = 0.30, thres.high = 0.95)
    W <- PCAmat (rCAM)
    W <- PCAmat(slot(rCAM, "PrepResult"))
```

    ratMix3 Gene expression data downsampled from GSE19380
    
## Description

Rat brain, liver and lung biospecimens derived from one animal at the cRNA homogenate level in different proportions. 3 technical replicates each. We downsample the original data to 10000 probes/probesets and 7 mixtures. Proportions used in experiments and pure expression profiles are also included.

## Usage

data(ratMix3)

## Format

A list with three matrices: mixture profiles $(X)$, mixing proportions $(A)$ and pure profiles $(S)$.

## References

Shen-Orr et al. (2010) Nat Methods 2010 Apr;7(4):287-9. PMID: 20208531

```
redoASest Re-estimate A,S matrix
```


## Description

This function re-estimates proportion and expression matrix iteratively by Alternating Least Square (ALS) method. The initial values are from markers or known proportion matrix or known expression matrix,

## Usage

redoASest(data, MGlist, $A=$ NULL, $S=$ NULL, generalNMF $=$ FALSE, maxIter $=2$, methy $=$ FALSE)

## Arguments

| data | A data set that will be internally coerced into a matrix. Each row is a gene <br> and each column is a sample. data should be in non-log linear space with non- <br> negative numerical values (i.e. >=0). Missing values are not supported. All-zero <br> rows will be removed internally. |
| :--- | :--- |
| MGlist | A list of vectors, each of which contains CAM-detected markers and/or prior <br> markers for one subpopulation. |
| A | Initial proportion matrix. If NULL, it will be estimated from initial expression <br> matrix. If initial expression matrix is also NULL, it will be estimated from <br> MGlist using AfromMarkers. |
| S | Initial expression matrix. If NULL, it will be estimated from initial proportion <br> matrix. |
| maxIter | If TRUE, the decomposed proportion matrix has no sum-to-one constraint for <br> each row. Without this constraint, the scale ambiguity of each column vector in <br> proportion matrix will not be removed. The default is FALSE. <br> maximum number of iterations for Alternating Least Square (ALS) method. The |
| methy | default is 2. If zero, ALS is not applied. |
| Should be TRUE when dealing with methylation data, whose expression levels |  |
| are confined between 0 and 1. |  |

## Details

If only markers are provided, they are used to estimate initial proportion matrix and then expression matrix. If proportion matrix or expression matrix is provided, it will be treated as initial matrix to estimate the other one. Then Alternating Least Square (ALS) method is applied to estimate two matrix alternatively. Note only markers' squared errors will be counted in ALS, which facilitates (1) faster computational running time and (2) a greater signal-to-noise ratio owing to markers' discriminatory power.
This function can be used to refine CAM estimation or perform supervised deconvolution. Note that allowing too many iterations may bring the risk of a significant deviation from initial values.

## Value

A list containing the following components:

```
Aest Proportion matrix after re-estimation and possible refinement.
Sest expression matrix after re-estimation and possible refinement.
mse Mean squared error (i.e. mean of reconstruction errors) for input markers
```


## Examples

```
#obtain data and run CAM
data(ratMix3)
data <- ratMix3$X
rCAM <- CAM(data, K = 3, dim.rdc= 3, thres.low = 0.30, thres.high = 0.95)
#obtain marker genes detected by CAM for estimating A
MGlist <- MGsforA(rCAM, K = 3)
```

```
#Re-estimation based on marker list
rre <- redoASest(data, MGlist, maxIter = 10)
Aest <- rre$Aest #re-estimated A matrix
Sest <- rre$Sest #re-estimated S matrix
#Re-estimation with initial A matrix
rre <- redoASest(data, MGlist, A=ratMix3$A, maxIter = 10)
#Re-estimation with initial S matrix
rre <- redoASest(data, MGlist, S=ratMix3$S, maxIter = 10)
```

```
reselectMG Reselect markers by thresholding
```


## Description

This function generates a new list of markers based on initially detected markers by CAM and/or prior markers.

## Usage

reselectMG(data, MGlist, fc.thres = "q0.5", err.thres = NULL)

## Arguments

data A data set that will be internally coerced into a matrix. Each row is a gene and each column is a sample. data should be in non-log linear space with nonnegative numerical values (i.e. $>=0$ ). Missing values are not supported. All-zero rows will be removed internally.
MGlist A list of vectors, each of which contains CAM-detected markers and/or prior markers for one subpopulation.
fc.thres The lower threshold of fold change to select markers, an absolute value (e.g. 10) or a quantile value after 'q' (e.g. 'q0.5', the median of fold changes of one subpopulation's input markers). Each subpopulation can have its own threshold if a vector is provided. The default is 'q0.5'. If NULL, still use the input markers.
err.thres The upper threshold of reconstruction error to select markers, an absolute value or a quantile value after 'q' (e.g. 'q0.5', the median of reconstruction errors of one subpopulation's input markers; 'q1.2', the maximum error times 1.2 ). Each subpopulation can have its own threshold if a vector is provided. The default is NULL, which means no such a threshold is applied.

## Details

Considering some meaningful markers may be mistakenly filtered by preprocessing and thus missed by CAM, this function use the input marker gene list to estimate proportions by AfromMarkers and then estimate expression levels. Next, a new list of markers are generated by fold change threshold and reconstruction error threshold.

The input marker genes could also be from other supervised detection and/or from literatures. This function reselects a list of marker genes based on the input.

## Value

A list of vectors, each of which contains new selected markers for one subpopulation.

## Examples

```
#obtain data and run CAM
data(ratMix3)
data <- ratMix3$X
rCAM <- CAM(data, K = 3, dim.rdc= 3, thres.low = 0.30, thres.high = 0.95)
#obtain marker genes detected by CAM with a fixed K
MGlist <- MGsforA(rCAM, K = 3)
#Reselect markers from all genes
MGlist.re <- reselectMG(data, MGlist, fc.thres='q0.5')
MGlist.re <- reselectMG(data, MGlist, fc.thres='q0.5', err.thres='q0.95')
```

| sffsHull | Sequential Forward Floating Selection (SFFS) to approximate convex <br> hull |
| :--- | :--- |

## Description

This function detects the corners of convex hull by greedy search. It will be used to reduce the number of candidate corners and thus reduce the time complexity in the further exhaustive search by cornerSort.

## Usage

sffsHull(Xall, Aall, Kmax, deltaK = 8)

## Arguments

Xall Data in a matrix. Each column is a data point. The cost is computed based on all data points.

Aall Candiatie corners in a matrix. Each column is a candidate corner.
Kmax The target number of corners to be selected.
deltaK The extra number of corners that need to be searched. The default is 8 and will be truncated based on all the available corners. SFFS runs until a corner set of cardinality (Kmax + deltak) is obtained. The set of cardinality Kmax might be improved during backtracking from extra corners.

## Details

The Sequential Floating Forward selection (SFFS) is one of greedy search methods for feature selection. With sum of margin-of-errors as cost function and candidate corners as features, SFFS is used to select best Kmax corners to form an approximated hull. The best subset of candidate corners is initialized as the empty set and at each step a new corner is added. After that, the algorithm searches for corner that can be removed from the best subset until the cost function does not decrease.

## Value

A list with length (Kmax + deltak). Each component is a vector of the corner indices of the SFFSselected subset with certain cardinality.

## Examples

```
data <- matrix(c(0.1,0.2,1.0,0.0,0.0,0.5,0.3,
            0.1,0.7,0.0,1.0,0.0,0.5,0.3,
            0.8,0.1,0.0,0.0,1.0,0.0,0.4), nrow =3, byrow = TRUE)
rsffs <- sffsHull(data, data, 3)
rsffs <- sffsHull(data, data[,1:5], 3)
```


## simplexplot The plot of scatter simplex

## Description

This function shows scatter simplex of mixture expressions.

## Usage

```
simplexplot(data, A, MGlist = NULL, data.extra = NULL,
    corner.order = NULL, col = "gray", pch = 1, cex = 0.8,
    mg.col = "red", mg.pch = 1, mg.cex = 1.2, ex.col = "black",
    ex.pch = 19, ex.cex = 1.5, ...)
```


## Arguments

$$
\begin{array}{ll}
\text { data } & \begin{array}{l}
\text { A data set that will be internally coerced into a matrix. Each row is a gene } \\
\text { and each column is a sample. Data should be in non-log linear space with non- } \\
\text { negative numerical values (i.e. >=0). Missing values are not supported. All-zero } \\
\text { rows will be removed internally. }
\end{array} \\
\text { A } & \begin{array}{l}
\text { Prior/Estimated proportion matrix. }
\end{array} \\
\text { MGlist } & \begin{array}{l}
\text { A list of vectors, each of which contains known markers and/or CAM-detected } \\
\text { markers for one subpopulation. }
\end{array} \\
\text { data.extra } & \begin{array}{l}
\text { Extra data points to be shown in the simplex plot, e.g. the points associated with } \\
\text { prior/estimated proportion vectors. The format should be consistent with data, } \\
\text { so prior/estimated proportion matrix needs to be transposed before as the input. }
\end{array}
\end{array}
$$

| corner.order | The order to show simplex corners counterclockwise. |
| :--- | :--- |
| col | The color for data points. The default is "gray". |
| pch | The symbol/character for data points. The default is 1. |
| mg.col | The symbol/character expansion for data points. The default is 0.8. |
| mg.pch | The colors for marker genes. Marker genes of one subpopulation could have <br> their own color if a vector is provided. The default is "red". |
| mg.cex | The symbols/characters for marker genes. Marker genes of one subpopulation <br> could have their own symbol/character if a vector is provided. The default is 1. |
| ex.col | The symbol/character expansion for marker genes. The default is 1.2. |
| The colors for extra data points. Each data point could have its own color if a |  |
| ex.pch | The symbols/characters for extra data points. Each data point could have its own <br> symbol/character if a vector is provided. The default is 19. |
| ex.cex | The symbol/character expansion for extra data points. The default is 1.5. |
| $\ldots$ | All other arguments are passed to the plotting command. |

## Details

This function can show the scatter simplex and detected marker genes in a 2D plot. The corners in the high-dimensional simplex will still locate at extreme points of low-dimensional simplex. These corners will follow the order set by corner. order to display in the plot counterclockwise.

## Value

A plot to the current device.

## Examples

```
#obtain data, A matrix, marker genes
data(ratMix3)
data <- ratMix3$X
A <- ratMix3$A
pMGstat <- MGstatistic(ratMix3$S, c("Liver","Brain","Lung"))
pMGlist.FC <- lapply(c("Liver","Brain","Lung"), function(x)
    rownames(pMGstat)[pMGstat$idx == x & pMGstat$OVE.FC > 10])
#plot simplex for data
simplexplot(data, A)
simplexplot(data, A, MGlist = pMGlist.FC) #Color marker genes in the plot
simplexplot(data, A, MGlist = pMGlist.FC,
    data.extra = t(A)) #show the location of proportion vectors in the plot
#set different corner order and colors
simplexplot(data, A, MGlist = pMGlist.FC, corner.order = c(2,1,3),
    col = "blue", mg.col = c("red","orange","green"))
```


## Description

This function reduces data dimension by loading matrix and then project dimension-reduced data to the hyperplane orthogonal to $c(1,0, \ldots, 0)$, i.e., the first axis in the new coordinate system..

## Usage

XWProj(data, W)

## Arguments

data A data set that will be internally coerced into a matrix. Each row is a gene and each column is a sample. Missing values are not supported. All-zero rows will be removed internally.
W The matrix whose rows are loading vectors; should be obtained from CAM/CAMPrep function with accessor method PCAmat.

## Details

This function can project gene expression vectors to simplex plot generated by CAM/CAMPrep. Using slot Xproj in "CAMPrepObj" can only show the simplex of genes after filtering. This function helps observe all genes in simplex plot.

## Value

The data after perspective projection.

## Examples

```
#obtain data
data(ratMix3)
data <- ratMix3$X
#preprocess data
rPrep <- CAMPrep(data, dim.rdc = 3, thres.low = 0.50, thres.high = 0.90)
#obtain simplex
Xproj <- XWProj(data, PCAmat(rPrep))
#plot simplex in 3d space
#plot3d(Xproj[,-1]) #The first dimension is constant after projection
```


## Index

```
AfromMarkers, 2, 3, 21, 22
Amat (AS-accessor), 4
Amat,CAMASObj-method (AS-accessor), 4
Amat,CAMObj-method (AS-accessor), 4
AS-accessor,4
CAM, 2, 5, 8, 10, 13, 15, 17, 22, 26
CAMASest, 2, 6, 7, 7, 11, 15
CAMASObj, 4, 7, 8, 11
CAMASObj (CAMASObj-class), }
CAMASObj-class,9
CAMMGCluster, 2, 6-8, 10, 11, 17
CAMMGObj, 7, 8, 10,11
CAMMGObj (CAMMGObj-class), 11
CAMMGObj-class, 11
CAMObj, 4, 6, 19
CAMObj (CAMObj-class), 11
CAMObj-class, 11
CAMPrep, 2, 6, 8, 10, 11, 12, 17,26
CAMPrepObj, 6, 8, 10, 11, 13, 19, 26
CAMPrepObj (CAMPrepObj-class), 14
CAMPrepObj-class,14
cornerSort, 14,23
debCAM (debCAM-package), 2
debCAM-package, 2
kmeans, 6, 12
l1median, 3
lofactor, 6,12
MDL, 2, 15, 15
MDLObj, 15, 16
MDLObj (MDLObj-class), 16
MDLObj-class, 16
MGsforA, 17
MGstatistic, 2, 17,18
PCAmat, 19, 26
PCAmat, CAMObj-method (PCAmat), 19
```

PCAmat, CAMPrepObj-method (PCAmat), 19
plot, MDLObj, missing-method (MDL), 15
ratMix3, 20
redoASest, 20
reselectMG, 22
sffsHull, 23
simplexplot, 24
Smat (AS-accessor), 4
Smat, CAMASObj-method (AS-accessor), 4
Smat, CAMObj-method (AS-accessor), 4
XWProj, 26

